

# Security Analysis of Safety Critical and Control Systems

# Outline

- Introduction
- Security Modeling Process
- Petri nets
- A Case Study
- Using Petri net for security analysis
- Conclusions

# Introduction

- Software has become an integral part of everyday system upon which the million of live depends.
- In early stage software into safety critical environment, were used to only expand the performance, flexibility and efficiency of systems. But now days it is major components consider for safety purpose.
- Problem of security and safety become important when these critical applications include software where consequence of failure of software are serious and may grave danger to human life and property.

# Introduction

**Safety critical system** is a system where human safety is dependent upon the correct operation of system. If the failure of a system could lead to consequences that are determined to be unacceptable then the system is safety critical.



a) Railway



d) Airbag



b) medical system



c) Nuclear power plants



e) Airspace

# Introduction

Digital technologies such as computers, control systems, and data networks currently play essential roles in modern nuclear power plants (NPPs). These digital technologies make the operation of NPPs more convenient and economical; however, they are inherently susceptible to cyber-attacks.

- In 2003, the enterprise and control networks of the Davis-Besse NPP in the US were shut down because of an infection by the Slammer worm.
- In 2006, the instrumentation and control (I&C) systems of the Browns Ferry NPP in the US state of Alabama were disabled because of a digital network problem; therefore, an operator shut down its operation manually.
- In addition, in 2010, a malicious code called Stuxnet damaged the Natanz nuclear power facility in Iran.



According to the Dr. Rajeswari Pillai Rajagoplam is senior Fellow at the Observer Research Foundation, New Delhi in her article “Nuclear Research in India”

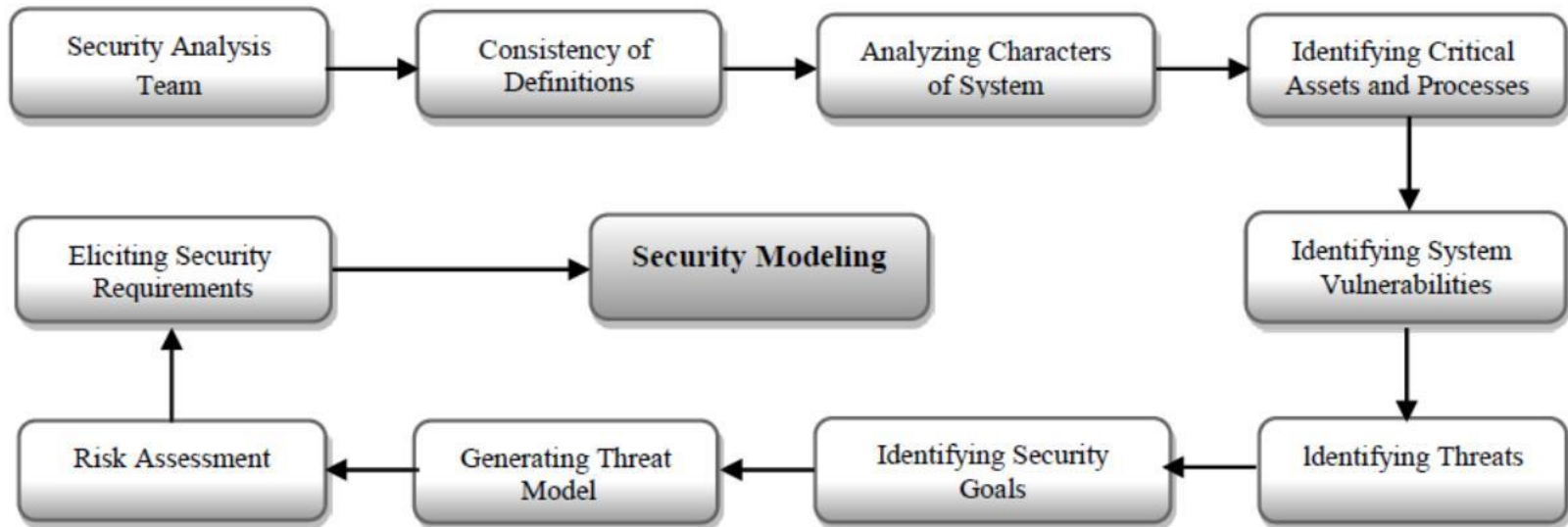
One of the more probable threats to Indian nuclear facilities could come in the form of cyber attacks. The capacity of terrorist groups to use cyber tools to attack a nuclear installation is far higher as compared to other attacks. As more and more systems rely on computer networks, cyber attacks have grown to be a major threat to India's nuclear installations.



Thomas Franch is Senior Vice President of Reactors and Services for AREVA, Inc., North America

- Across the nation, nuclear plants are being licensed to operate for longer periods of time and are transitioning from analog to digital systems for increased safety and performance. While this transition to digital technology is increasing the capability, longevity, safety and reliability of America's nuclear plants, the need to integrate cybersecurity measures is a necessity.
- Protecting the U.S. nuclear power infrastructure from exploitation and cyberattacks perpetrated against critical system networks is an industry challenge.

# Security Modeling Process



**Figure 1. Security Modeling Process**



# Petri nets

- concurrent, asynchronous, distributed, parallel, nondeterministic and/or stochastic systems
- graphical tool
  - visual communication aid
- mathematical tool
  - state equations, algebraic equations, etc
- communication between theoreticians and practitioners

# Petri nets History

- **1962:** C.A. Petri's dissertation (U. Darmstadt, W. Germany)
- **1970:** Project MAC Conf. on Concurrent Systems and Parallel Computation (MIT, USA)
- **1975:** Conf. on Petri Nets and related Methods (MIT, USA)
- **1979:** Course on General Net Theory of Processes and Systems (Hamburg, W. Germany)
- **1980:** First European Workshop on Applications and Theory of Petri Nets (Strasbourg, France)
- **1985:** First International Workshop on Timed Petri Nets (Torino, Italy)

# Petri nets Applications

- **performance evaluation**
- **communication protocols**
- distributed-software systems
- distributed-database systems
- concurrent and parallel programs
- industrial control systems
- discrete-events systems
- multiprocessor memory systems
- dataflow-computing systems
- fault-tolerant systems
- etc, etc, etc

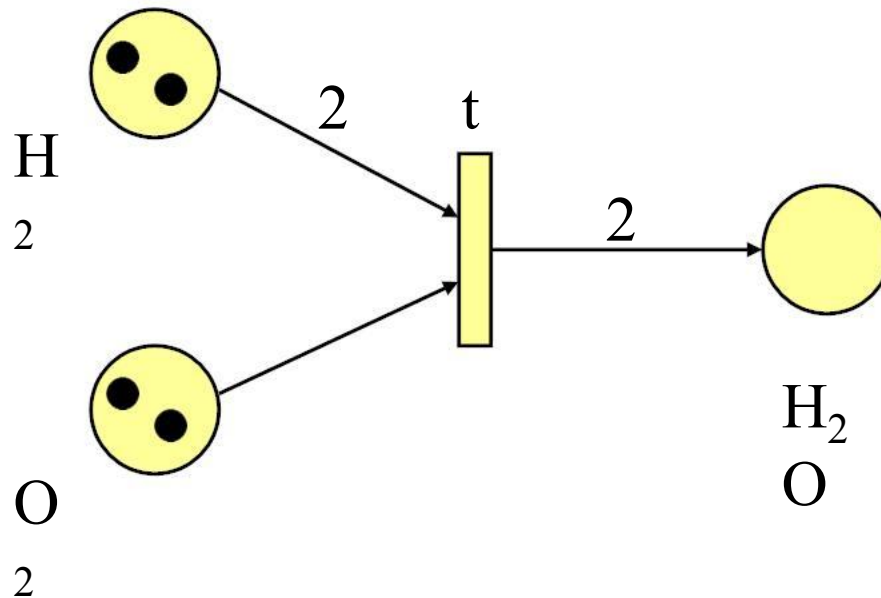
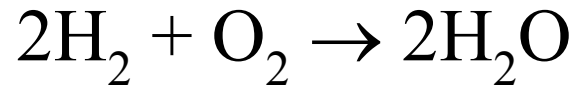
# Petri nets Definition

- Directed, weighted, bipartite graph
  - places
  - transitions
  - arcs (places to transitions or transitions to places)
  - weights associated with each arc
- Initial marking
  - assigns a non-negative integer to each place

# Petri nets Definition

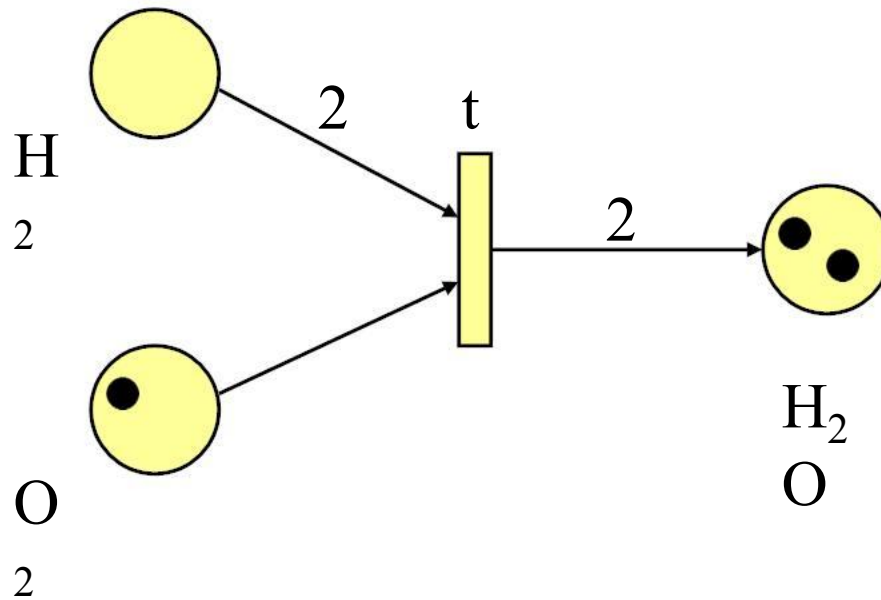
- A transition  $t$  is enabled if each input place  $p$  has at least  $w(p,t)$  tokens
- An enabled transition may or may not fire
- A firing on an enabled transition  $t$  removes  $w(p,t)$  from each input place  $p$ , and adds  $w(t,p')$  to each output place  $p'$

# Petri nets Firing example

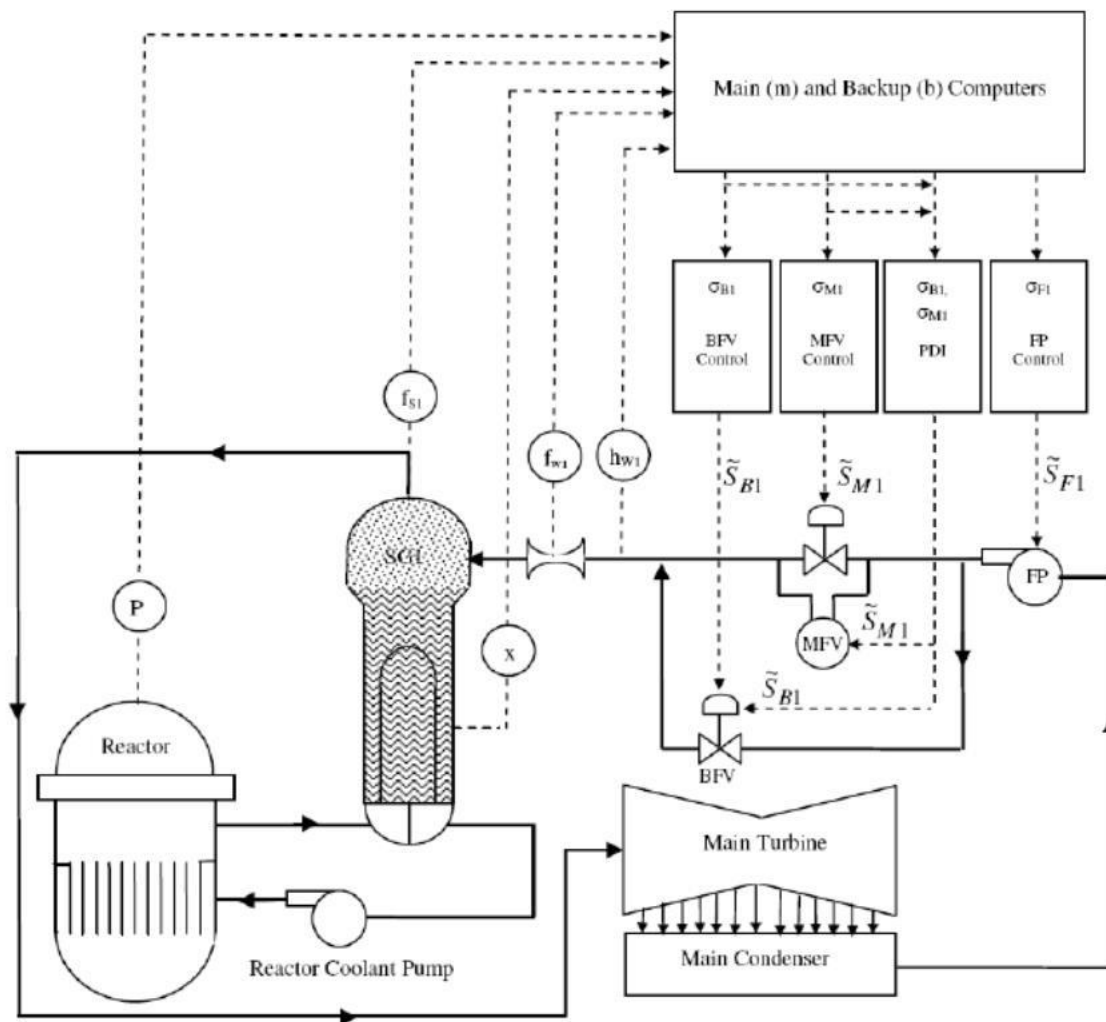


# Petri nets Definition

- $2\text{H}_2 + \text{O}_2 \rightarrow 2\text{H}_2\text{O}$

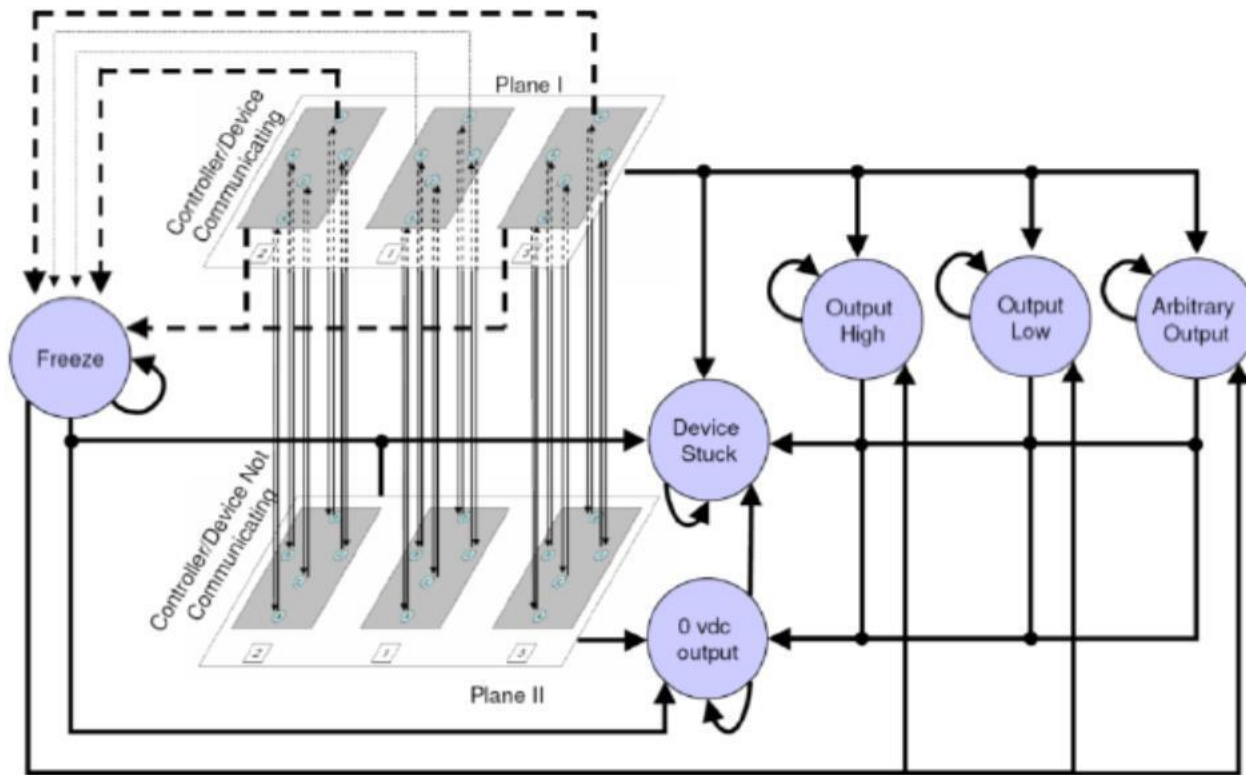


# A Case Study: Digital Feed Water Control System

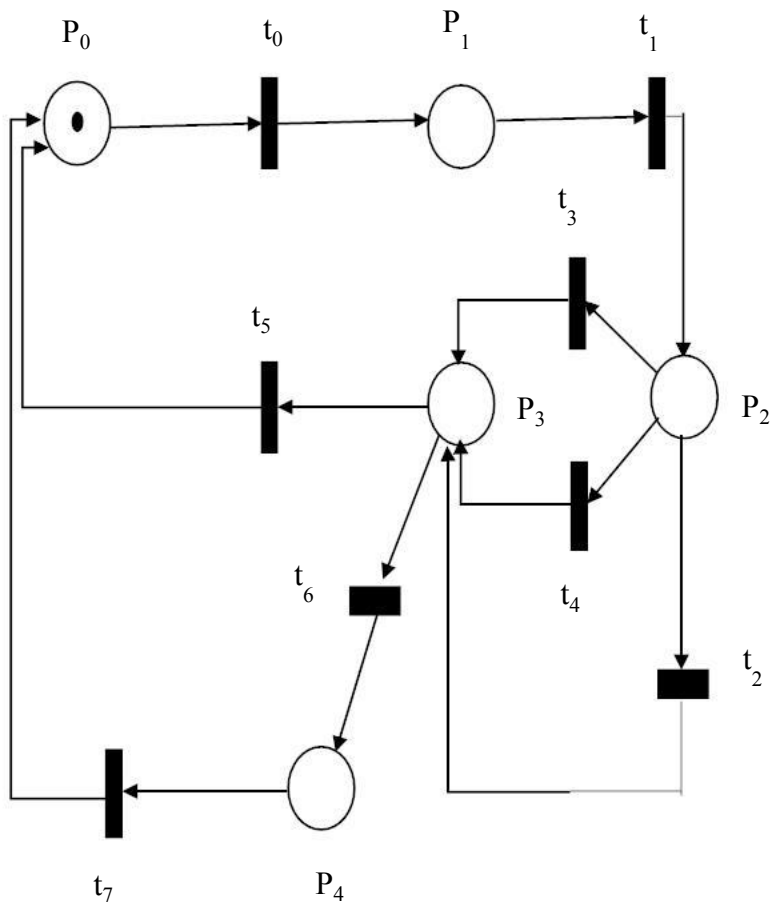




# Computer-controller-actuated devices interaction in DFWCS



# Generate model

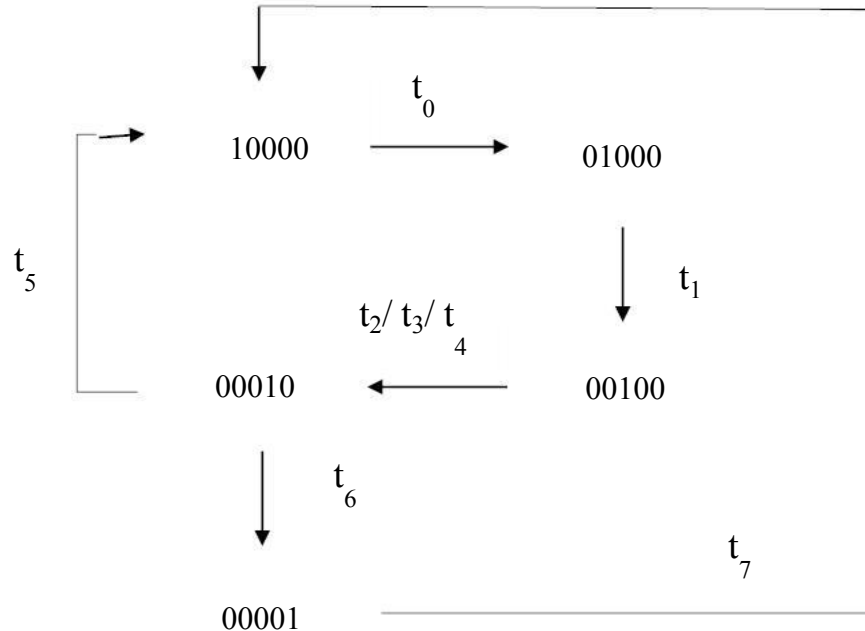


Places	Description
P <sub>0</sub>	FWS is in ready state
P <sub>1</sub>	Computer (MC or BC) receive deviated value
P <sub>2</sub>	Controller receive error signal(deviated value)
P <sub>3</sub>	Actuator operates(according to the input)
P <sub>4</sub>	Actuator in stuck state

Transitions	Description
t <sub>0</sub>	SG level deviated from normal limit
t <sub>1</sub>	Error signal(deviated value) send to the controller
t <sub>2</sub>	Trigger normal open to actuator
t <sub>3</sub>	Controller recognized failure of computer and send previous correct (freeze)value to the actuator device
t <sub>4</sub>	Controller does not recognized failure of MC/BC and send false value (high /low/ arbitrary) to the actuator device
t <sub>5</sub>	System reset
t <sub>6</sub>	Actuator stuck
T <sub>7</sub>	Repair

# Behavioral and Structural analysis

**Behavioral properties:** Behavioral properties depend on the initial marking of the net. In this phase the behavioral properties for the created PN is validated with respect to the three basic properties: **reachability**, **boundedness and liveness from the reachability graph.**



Structure properties are depending on the topological structure of the net, namely **p-invariant and siphons**. P-invariant is corresponds to a set of places whose weighted token count is a constant for any reachable marking.

# P-invariant

- Calculate incidence matrix

$$A = D^- - D^+$$

$$D^- = \begin{bmatrix} & t_0 & t_1 & t_2 & t_3 & t_4 & t_5 & t_6 & t \\ p_0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ p_1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ p_2 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ p_3 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 0 \\ p_4 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \end{bmatrix}$$

$$D^+ = \begin{bmatrix} & t_0 & t_1 & t_2 & t_3 & t_4 & t_5 & t_6 & t \\ p_0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ p_1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ p_2 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 0 \\ p_3 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 0 \\ p_4 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

# P-invariant

- Calculate incidence matrix

$$A = D^- - D^+$$

$$A = \begin{bmatrix} & t_0 & t_1 & t_2 & t_3 & t_4 & & t_5 & t_6 & t_7 \\ p_0 & -1 & 0 & 0 & 0 & 0 & & 1 & 0 & 1 \\ p_1 & 1 & -1 & 0 & 0 & 0 & & 0 & 0 & 0 \\ p_2 & 0 & 1 & -1 & -1 & -1 & & 0 & 0 & 0 \\ p_3 & 0 & 0 & 1 & 1 & 1 & & -1 & -1 & 0 \\ p_4 & 0 & 0 & 0 & 0 & 0 & & 0 & 1 & -1 \end{bmatrix}$$

# P-invariant calculation

The order of places in the matrix is row based  $P = \{P_0, P_1, P_2, P_3, P_4\}$  and the order of transitions is column based  $T = \{t_0, t_1, t_2, t_3, t_4, t_5, t_6, t_7\}$ .

$$\begin{bmatrix} -1 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 1 & -1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & -1 & -1 & -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 1 & -1 & -1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & -1 \end{bmatrix}$$

2 Step

$$\begin{bmatrix} -1 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 1 & -1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & -1 & -1 & -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 1 & -1 & -1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & -1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

3<sup>rd</sup> Step

$$\begin{bmatrix} 0 & -1 & 0 & 0 & 0 & 1 & 0 & 1 \\ 0 & 1 & -1 & -1 & -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 1 & -1 & -1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & -1 \end{bmatrix} \begin{bmatrix} 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

4<sup>th</sup> step

$$\begin{bmatrix} 0 & 0 & -1 & -1 & -1 & 1 & 0 & 1 \\ 0 & 0 & 1 & 1 & 1 & -1 & -1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & -1 \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

5<sup>th</sup> step

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & -1 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & -1 \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

6<sup>th</sup> step  $[0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0] \begin{bmatrix} 1 & 1 & 1 & 1 & 1 \end{bmatrix}$

P-invariant is  $x = [1 \ 1 \ 1 \ 1 \ 1]$

# T-invariant

- T-invariant

$$\begin{bmatrix} -1 & 1 & 0 & 0 & 0 \\ 0 & -1 & 1 & 1 & 1 \\ 0 & 0 & -1 & 1 & 0 \\ 0 & 0 & -1 & 1 & 0 \\ 1 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 & 1 \\ 1 & 0 & 0 & 0 & -1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

- 2step

$$\begin{bmatrix} 0 & 1 & 0 & -1 & 0 \\ 0 & 1 & 0 & 0 & -1 \\ 0 & -1 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

- 3<sup>rd</sup> step

$$\begin{bmatrix} 0 & 0 & 1 & -1 & 0 \\ 0 & 0 & 1 & 0 & -1 \\ 0 & 0 & -1 & 1 & 0 \\ 0 & 0 & -1 & 1 & 0 \\ 0 & 0 & -1 & 1 & 0 \end{bmatrix} \begin{bmatrix} 1 & 1 & 0 & 0 & 0 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \end{bmatrix}$$

- 4<sup>th</sup> step

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & -1 \\ 0 & 0 & 0 & 1 & -1 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 & 0 & 0 & 1 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 & 0 & 0 & 1 \\ 1 & 1 & 0 & 1 & 0 & 0 & 0 & 1 \\ 1 & 1 & 0 & 1 & 0 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \end{bmatrix}$$

- 5<sup>th</sup> step

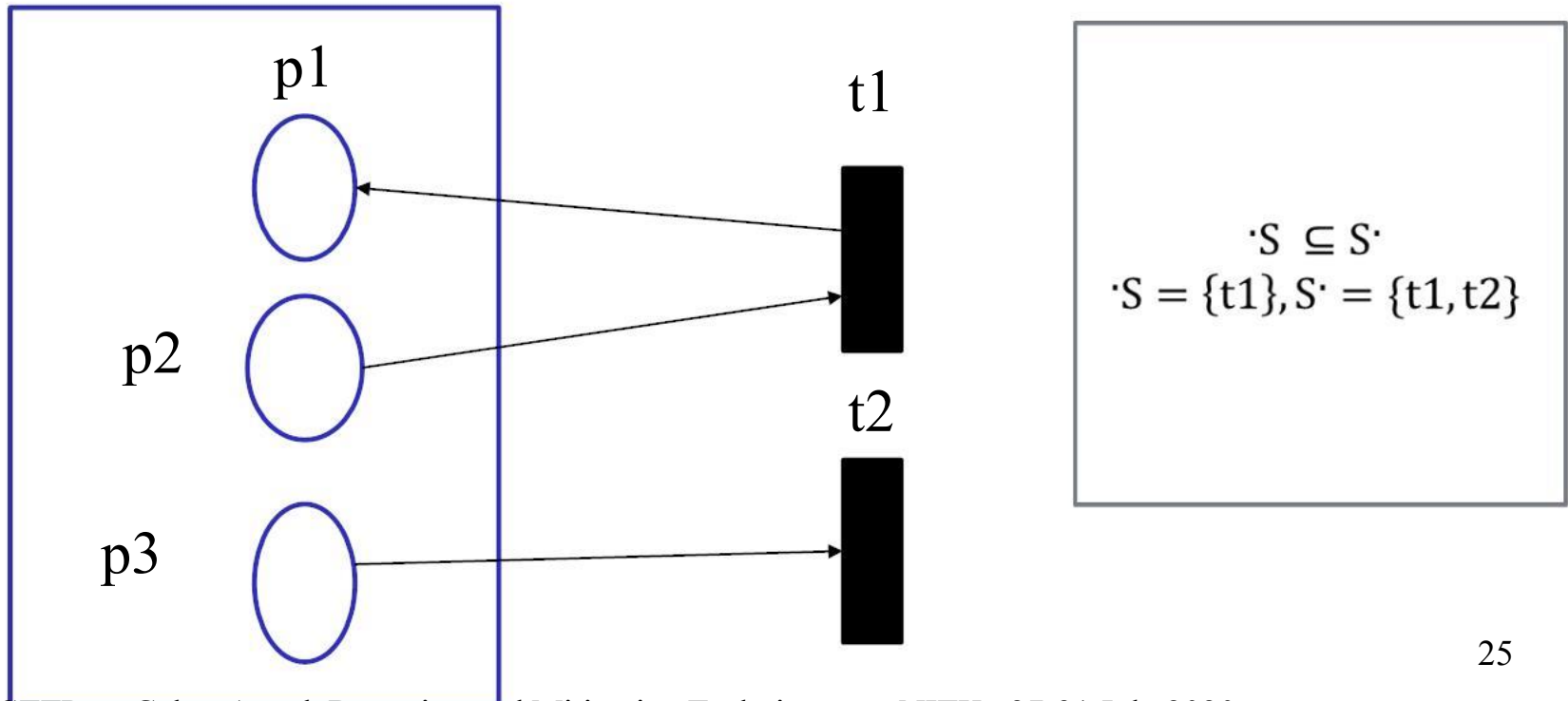
$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 & 0 & 0 & 1 & 0 & 0 \\ 1 & 1 & 0 & 1 & 0 & 0 & 1 & 1 \\ 1 & 1 & 1 & 0 & 0 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 & 0 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \end{bmatrix}$$

T-invariants  $y_1$   
 $= [11100100]$ ,  
 $y_2 = [11010011]$ ,  $y_3 =$   
 $[11100011]$ ,  $y_4 =$   
 $[11010100]$ ,  $y_5 =$   
 $[11001100]$



# SIPHON

The siphon is used for the structural analysis of PN. A non-empty sub-set of places  $S \subseteq P$  is called a siphon if  $\cdot S \subseteq S'$  i.e, a set of transition having an output place in  $S$  has an input place in  $S$ . A siphon is called to be minimal if it does not contain any other siphon as a proper subset. A minimal siphon that does not comprise the support of any P-invariant is called a strict minimal siphon. A siphon  $S$  which is controlled by P-invariants can never be emptied. It is called to be invariant-controlled by P-invariant  $I$  under  $M_0$  if  $I^T \bullet M_0 > 0$  and  $\|I\|^+ \subseteq S$ . The emptiness of minimal siphon leads to the deadlock of the net.



# Conclusions

- Software security is a key part in software quality
- Software security improvement is hard
- There are no generic models
- Measurement is very important for finding the correct model
- Using PN for security analysis

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# Thank You!

`lalit.singh.poo(at)gmail.com`